

Translated from the original in spanish

Original article

Movement of water in the wood during drying discreet model

Movimiento del agua en la madera durante el secado. Modelo discreto

Movimento da água na madeira durante o secado. Padrão discreto

Inés González Cruz¹* https://orcid.org/0000-0001-7900-8547

Luisberis Velázquez Abad ² https://orcid.org/0000-0001-6303-9664

Daniel Álvarez Lazo¹ https://orcid.org/0000-0001-7627-0152

¹Universidad de Pinar del Río "Hermanos Saíz Montes de Oca". Pinar del Río, Cuba. ²Universidad Católica del Norte. Antofagasta. Chile.

*Correspondence author: ines@upr.edu.cu

Received: August 20th, 2020. **Approved:** September 20th, 2020.

ABSTRACT

The knowledge of the factors that produce the deformations of the wood can help to a suitable selection of the material before its sawing. One way to address the problem of deformation is with the understanding of the mechanisms that regulate it. The objective of the work was to describe the behavior of the movement of water during the drying of wood as an influential factor in the deformations of the same during this process from a theoretical model, which unifica features Newton's dynamics of a system of particles and schemes of the methods of the finite elements. This model allows to establish in detail the qualitative and quantitative influence of the humidity in the nature of the deformations, which facilitates to value the experimental results, to make predictions in the practical activity, and to obtain a considerable saving of resources and time.

Keywords: Moisture; Wood; Drying; Model.

RESUMEN

El conocimiento de los factores que producen las deformaciones de la madera puede ayudar a una selección adecuada del material antes de su aserrado. Una manera de enfrentar el problema de las deformaciones es con el entendimiento de los mecanismos que la regulan. El objetivo del trabajo fue describir el comportamiento del movimiento del agua durante el secado de la madera, como factor influyente en las deformaciones de la misma durante este proceso, a partir de un modelo teórico, que uniﬕ ca rasgos de la dinámica de Newton de un sistema de partículas y esquemas propios de los métodos de los elementos ﬕ nitos. Este modelo permite establecer en detalle la inï¬,uencia cualitativa y cuantitativa de la humedad en la naturaleza de las deformaciones, lo que permite entender los resultados





experimentales y realizar predicciones, que implican en la actividad práctica, un ahorro considerable de recursos y de tiempo.

Palabras clave: Humedad; Madera; Modelo; Secado.

RESUMO

O conhecimento dos fatores que originam deformações na madeira pode ajudar à seleção adequada do material antes do serrado. Um modo de confronto do problema das deformações é atingindo os mecanismos que regulam as. A finalidade do trabalho foi descrever o comportamento do movimento da água durante o secado da madeira, como fator agente nas deformações da mesma durante este processo, a partir dum padrão teórico, que associa rasgos da dinâmica de Newton de um sistema de partículas e desenhos próprios dos métodos dos elementos finitos. Este modelo permite estabelecer em minúcia, a influência qualitativa e quantitativa da humidade na natureza das deformações, o que promove perceber os resultados experimentais e realizar predições, que traem como consequências, na atividade prática, bom emprego de recursos e do tempo.

Palavras chave: Humidade; Madeira; Padrão; Secado.

INTRODUCTION

The consumption of large volumes of sawn wood in our country indicates as a fundamental need to increase the efficiency of the sawing industry, taking into account to minimize the contractions and other deformations that it presents after its drying, because in the construction the deformations that the sawn wood experiences affect its quality, being the most important property the swelling and the contraction (Álvarez *et al.*, 2013).

Contraction occurs only when the wood loses humidity below the saturation point of the ûbra (PSF). This point is an interesting fact for the structural and decorative uses of wood. It is accepted that for the practical use of all species the average value of the fibre saturation point is 30 %. (Álvarez, *et al.*, 2013). As a result of the movement of water during the drying process, the wood undergoes changes in its physical and mechanical properties (Sokolowskyy *et al.*, 2014).

The bound water is attached to the cell walls by very intense physical and chemical forces. During the drying process, first all the free water is removed and then some of the bound water is removed. The removal of the free water is carried out quickly and the energy consumption is relatively low, as the free water is very weakly bound to the wood. The wood begins to lose water until it reaches a point called: Fiber Saturation Point (FSP) in which it no longer has free water to lose. During this phase there are no dimensional changes in the wood, because the water that was inside the cells has been eliminated (Álvarez *et al.*, 2013).

Associated to the humidity changes there are deformations of the wood of *Pinus caribaea var. caribaea* (González-Cruz, 2008 and Guera *et al.*, 2020). According to Sokolowskyy *et al.* (2014), the application of mathematical modeling makes it possible to automate the analysis of the phenomena that occur during the drying process.





Different mathematical methods have been used to define the movement of water in the wood during drying, among which the works developed by Salinas *et al.*, (2010 and Salinas *et al.*, 2015), Pérez *et al.*, (2018), Montero *et al.*, (2020).

The treatment of deformations associated with humidity gradients during the drying process is traditionally described from a theoretical point of view using the Theory of Continuous Media (Ormarsson *et al.*, 2000). This working model, which considers the anisotropy and non-homogeneity of the medium, offers valuable results in the treatment of this phenomenon (deformations) but for its assumptions leaves out of reach the consideration of the discontinuous properties that are inherent to a medium as exceptional as wood (González-Cruz, 2008).

A different vision is proposed in this work: The study of the movement of water in wood during drying, using discrete models that make use of the Newtonian formulation of particle systems, which are widely used in physics to study the behavior of gases, liquids and solids using the methods of classical molecular dynamics. There is a significant knowledge of the peculiarities that these models allow to describe. To gain a better understanding of this phenomenon, a theoretical study of the movement of water during the drying process of the sawn wood of *Pinus caribaea* Morelet var. *caribaea*.

The objective of this study is to describe the behavior of the movement of water in the sawn wood of *Pinus caribaea* Morelet var. *caribaea* from the theoretical model. This description provides important elements for the area of wood technology and the sawing industry (González-Cruz *et al.*, 2007; González-Cruz, 2008; Montero *et al.*, 2020), who considers that simulation is widely used to improve and optimize the drying process of wood.

MATERIALS AND METHODS

The basic idea of the discrete model starts from considering a portion of the material in small non-overlapping volumes or cells as done in the finite element methods. This portion should be represented schematically (Figure 1) by a grid in which each node is equivalent to a given elementary volume of the material studied, which are linked by segments or links, representing the contact surfaces between adjacent cells. These nodes will have associated the physical properties that we describe in this case: the position radius vector (*ri*) of the i-ésimo node will represent from now on the position of its center of mass, to which is also associated the mass (*mi*), volume (*vi*) or humidity content h (*hi*).

The links form the basis of the dynamic mechanism by which the nodes interact by modifying the humidity during the diffusion process that takes place during drying.



Figure 1. - Discrete recreation of a piece of sawn wood in which only two species of nodes have been considered (marked with different colors), modeling what will be the characteristic ring structure of this material





In order to have a dense representation of the nodes/cells to establish the reticular model of a piece of sawn wood, a grid formed by parallel planes in the shape of a regular triangular net was used. Each node of this network has 12 close neighboring nodes, whose links with the first one defines the directions of application of the interactions and of water transport (diffusion) during the drying process.

To study the dynamics of water during drying, we assume pieces of sawn wood with sections of $(10 \times 10 \times 100)$ mm, which were recreated in the discrete model by a grid formed by $10 \times 11 \times 100 = 11000$ nodes.

Movement of bound water

This study is limited to the dynamics of bound water under the assumption that the initial state of the samples is close to the saturation point of the ûbra. In this case, the drying process of bound water takes place through a diffusion process (Gatica *et al.*, 2011; Montero *et al.*, 2020) which can be described in general by the Equation (1).

$$\frac{\partial \eta}{\partial t} = \frac{\partial}{\partial r^{\mu}} \left(D^{\mu \upsilon} \frac{\partial \eta}{\partial r^{\upsilon}} \right) \qquad (1)$$

 $D^{\mu u}$ — Diffusion tensor (non-homogeneous, anisotropic)

Reformulation of the diffusion in terms of the discrete model

The reformulation of the equations associated with the diffusion process in the continuous medium to the frame of the discrete model is established by assuming that the speed of change of the bound water content per unit volume in the i-ésimo node (particle) with volume (v_i) is subjected to the Equation (2).

$$\upsilon_{i}\frac{dh_{i}}{dt}=\sum_{j}\omega_{ij}\left(h_{j}-h_{i}\right) \tag{2}$$

Where ω_{ij} is the probability of transit of bound water through the link $_{ij}$, which satisfies the relation $\omega_{ij} = \omega_{ij}$ that guarantees that the contribution of the flujo of bound water coming from the j- ésimo node is equal to the partial loss that this last node has with that link.

This transit probability is assumed to be proportional to the area S_{ij} of the superûcie of contact between adjacent cells associated with the nodes involved in the link $J\omega_{ij} = S_{ij}.\beta_{ij}$, where β_{ij} is the transit probability per unit area.

The move to the continuum is made by considering the approximation h_j - $h_i = r_{ij} v_h$ where the terms from \hat{u}_{ujo} can be rewritten as follows (Equation 3).

$$\sum_{j} \omega_{ij} . r_{ij} . \nabla h = \sum_{j} S_{ij} . J_{ij}$$
(3)

Where $S_{ij} = S_{ij}$. e_{ij} vector area associated with the link(ij) whose normal vector $e_{ij} = r_{ij}/|r_{ij}|$ is directed along the link in the direction of the j-ésimo node, and j_{ij} (Equation 4).

http://cfores.upr.edu.cu/index.php/cfores/article/view/658



ISSN: 1996–2452 RNPS: 2148 Revista Cubana de Ciencias Forestales. 2020; September-December 8(3): 468-477



$$J_{ij} = -\beta_{ij} \cdot e_{ij} (rij \cdot \nabla h), \qquad (4)$$

the resulting ûujo humidity at the link address.

When entering the limit to the continuum (Equation 5).

$$\sum_{j} S_{ij} . J_{ij} \rightarrow \int_{\partial \Omega} J. ds = \int_{\Omega} div J d^{3} r \quad (5)$$

and

$$v_i \frac{dh_i}{dt} \rightarrow \int_\Omega \frac{\partial h}{\partial t} d^3 r$$

The continuity equation is deduced (6)

$$\partial h / \partial t + div J = 0$$
 (6)

There is a general linear relationship between flow and humidity gradient, as expressed by the equation (Equation 7).

$$J^{\mu} = -D^{\mu\nu} \frac{\partial h}{\partial r^{\mu}} \qquad (7)$$

The equations that describe this study were implemented computationally through the use of the FORTRAN programming language in order to perform the numerical analysis. The results derived from such studies were analyzed using the ORIGIN 6.0.

To study the influence of the environmental conditions that influence the dynamics of the drying process, the process was analyzed for two drying regimes with different values of humidity content at the border of the sawn pieces: the first for 3 %, corresponding to a low environmental humidity content such as those reached by kiln drying, and the second for 10 %, associated with what would be natural drying, also assumed by Ormarsson *et al.*, (2000).

RESULTS AND DISCUSSION

In general terms, only theoretical modeling allows to establish in detail the qualitative and quantitative influence of influential factors in the nature of the phenomenon studied, arriving at a deep understanding of it that not only allows to understand and explain experimental results; but also, to predict them.

Comparison between two drying regimes

It should be noted that humidity is a variable that was not experimentally controlled, so the results presented are model predictions derived from the numerical simulation of the phenomenon.





ISSN: 1996–2452 RNPS: 2148 Revista Cubana de Ciencias Forestales. 2020; September-December 8(3): 468-477



Figure 2. - Dynamic evolution of average humidity

Figure 2 shows the evolution of the drying process of sawn wood pieces in terms of average humidity for the two types of boundary conditions considered in this study. The time scale is referred to in units of the simulation. The horizontal lines indicate the level of humidity content corresponding to the PSF and the values at the borders ηf = 0 ,03 (3 %) and 0.10 (10 %) used in the numerical experiments.

The drying process runs faster the lower the ambient humidity, reaching a standard humidity content value of $\eta_{\text{prom}}=0$, 12 (12 %) involves a time two to three times longer, for a humidity content at the edge of the pieces $\eta f = 0$, 10 (10 %) than that involved for when $\eta f=0$,03. (3 %). This result is interpreted in a similar way to that obtained by Montero (2020) in the simulation of drying in *Eucalyptus nitens* using diffusion models.

Humidity behavior with the advance of drying

Figures 3 and 4 show the humidity content distributions for the average humidity values $\eta_{prom}=0.25$ (25 %); 0.18 (18 %); 0.15 (15 %) and 0.12 (12 %) obtained through the numerical simulation of the drying process of the sawn wood pieces. The regions where the humidity content is very close to the PSF are represented in black, with less intense grey representing the lower humidity values.









Figure 4. - Humidity distribution in the cross-section of the workpiece with the drying progress for a humidity content at the border of 10 %

It is interesting to verify the persistence of a central region with a humidity content very close to the saturation point of the fiber even for relatively low average humidity values ~ 0.15 (15%) corresponding to the drying process under low environmental humidity conditions (when η f=0.03), results similar to those obtained by Montero (2020).

These results clearly indicate that while the outer regions of the parts tend to shrink due to humidity loss, the central region with humidity close to the PSF is not subject to shrinkage processes, hence stresses associated with these humidity gradients arise between the outer and inner areas, Similar behavior was obtained in the mathematical modeling of conventional drying in European oak *Quercus pedonculae* wood by Sandoval-Torres, (2009) and in the simulation of stresses during the drying process, considering the variations of moisture in *Eucalyptus nitens* wood by Pérez *et al.* (2018).

These tensions may not cause significant deformations in the parts in these states, but they may lead to the formation of cracks and fractures in the sinus and surface of the material when these exceed the limits of resistance of the material, which should be more pronounced as the dimensions of the parts increase.

Although the drying process that takes place under conditions of ambient humidity that are not so low (in our case $\eta f=0,10$) is slower, it has the advantage of not causing great humidity tensions, since in this the drying occurs more homogeneously in the volume of the pieces, thus avoiding the appearance of high humidity gradients, a behavior that does not favor the appearance of cracks and fractures in the pieces

The greatest deformations should occur once these interior regions with high humidity values have disappeared, and the contractions are present in the entire volume of the pieces.





CONCLUSIONS

The theoretical modeling of the drying phenomenon using the discrete model makes it possible to analyze the behavior of the distribution of humidity content during the progress of drying, a study that leads to greater compression of the process.

While the outer regions of the parts tend to shrink due to humidity loss, the central region with humidity close to the PSF is not subject to shrinkage processes, hence tensions arise between the outer and inner areas.

The drying speed is higher for those regimes where the environmental humidity conditions are lower; but this fact has the disadvantage of causing greater humidity gradients between the borders and the interior of the pieces, causing the existence of tensions that can potentially cause cracks and fractures in their borders.

REFERENCES

GATICA, Y.A., SALINAS, C.H. y ANANIAS, R.A., 2011. MODELING CONVENTIONAL ONE-DIMENSIONAL DRYING OF RADIATA PINE BASED ON THE EFFECTIVE DIFFUSION COEFFICIENT. *Latin American Applied Research* [en línea], vol. 14, no. 2, pp. 183-189. [Consulta: 20 septiembre 2020]. Disponible en: https://revistas.uns.edu.ar/laar2/article/view/217.

GONZÁLEZ, I., ÁLVAREZ, D., QUINTERO, A., ALVES, A. y RODRÍGUEZ, J., 2007. Comportamiento de algunas propiedades físicas en la dirección radial de la madera de la especie de Pinus caribaea Morelet var. caribaea. *Revista Baracoa* [en línea], vol. 2, no. 1. ISSN 0138-6441. Disponible en: https://agris.fao.org/agrissearch/search.do?recordID=CU2010800039.

GONZÁLEZ-CRUZ, I., 2008. Análisis de las deformaciones de la madera aserrada de Pinus caribaea Morelet var. caribaea [en línea]. Tesis presentada en opción al grado científico de Doctora en Ciencias Forestales. Pinar del Río, Cuba.: Universidad de Pinar del Río «Hermanos Saíz Montes de Oca». Disponible en: https://agris.fao.org/agris-search/search.do?recordID=CU2011800029.

GUERA, O.G.M., SILVA, J.A.A. da, FERREIRA, R.L.C., ÁLVAREZ LAZO, D., BARRERO MEDEL, H., GUERA, O.G.M., SILVA, J.A.A. da, FERREIRA, R.L.C., ÁLVAREZ LAZO, D. y BARRERO MEDEL, H., 2019. Modelos matemáticos para la determinación del turno óptimo en plantaciones forestales. Madera y bosques [en línea], vol. 25, no. 1. 20 septiembre 2020]. ISSN 1405-0471. [Consulta: DOI 10.21829/myb.2019.2511636. Disponible en: http://www.scielo.org.mx/scielo.php?script=sci_abstract&pid=S1405-04712019000100209&lng=es&nrm=iso&tlng=es.

MONTERO, C., ROZAS, C. y PICANTE, C., 2020. Simulación del secado en madera de Eucalyptus usando modelos de difusión bajo condiciones unidimensionales e isotérmicas. *Scientia forestalis* [en línea], vol. 48, no. 126. Disponible en: https://www.ipef.br/publicacoes/scientia/nr126/2318-1222-scifor-48-126-e2957.pdf.

ORMARSSON, S., DAHLBLOM, O. y PETERSSON, H., 2000. A numerical study of the shape stability of sawn timber subjected to moisture variation. En: Company: SpringerDistributor: SpringerInstitution: SpringerLabel: Springernumber: 3publisher: Springer-Verlag, *Wood Science and Technology* [en línea], vol. 34, no.



ISSN: 1996-2452 RNPS: 2148 Revista Cubana de Ciencias Forestales. 2020; September-December 8(3): 468-477



3, pp. 207-219. [Consulta: 20 septiembre 2020]. ISSN 1432-5225. DOI 10.1007/s002260000042. Disponible en: https://link.springer.com/article/10.1007/s002260000042.

PÉREZ-PENA, N., CHÁVEZ, C., SALINAS, C. y ANANÍAS, R.A., 2018. Simulation of Drying Stresses in Eucalyptus nitens Wood. *BioResources* [en línea], vol. 13, no. 1, pp. 1413-1424. [Consulta: 20 septiembre 2020]. ISSN 1930-2126. Disponible en: https://ojs.cnr.ncsu.edu/index.php/BioRes/article/view

/BioRes 13 1 1413 Perez Pena Simulation Drying Stress Eucalyptus.

SALINAS, C., ANANIAS, R., GATICA, Y. y CHAVEZ, C., 2010. Simulation of the Dryng Stresses in Wood. Mecánica Computacional [en línea], vol. 29, no. 85, pp. 8347-8354. [Consulta: 20 septiembre 2020]. Disponible en: https://cimec.org.ar/ojs/index.php/mc/article/view/3602.

SALINAS, C., CHAVEZ, C., ANANIAS, R.A. y ELUSTONDO, D., 2015. Unidimensional Simulation of Drying Stress in Radiata Pine Wood. Drying Technology [en línea], vol. 33, no. 8, pp. 996-1005. [Consulta: 20 septiembre 2020]. ISSN 0737-3937. DOI 10.1080/07373937.2015.1012767. Disponible en: https://doi.org/10.1080/07373937.2015.1012767.

YURIY, P., IGOR, K. y YAROSLAV, S., 2014. Mathematical modeling of timber elasticviscous-plastic deformation in the wood drying process. Лесотехнический журнал [en línea], vol. 4, no. 2 (14). [Consulta: 20 septiembre 2020]. ISSN 2222-7962. Disponible en: https://cyberleninka.ru/article/n/mathematical-modeling-of-timberelastic-viscous-plastic-deformation-in-the-wood-drying-process.

Conflict of interests:

The authors declare not to have any interest conflicts.

Authors' contribution:

The authors have participated in the writing of the work and analysis of the documents.



This work is licensed under a Creative Commons Attribution-NonCommercial 4.0 International license Copyright (c) Inés González Cruz, Luisberis Velázquez Abad, Daniel Álvarez Lazo



http://cfores.upr.edu.cu/index.php/cfores/article/view/658